

BUILDING A STATE-OF-THE-ART MODEL CHECKER

— Sebastian Wolff —

Technische Universität Kaiserslautern

WHAT IS MODEL CHECKING?

- ▶ proving correctness
 - ▶ vs. testing
- ▶ w.r.t. a specification
- ▶ automated

AUTOMATED PROOFS

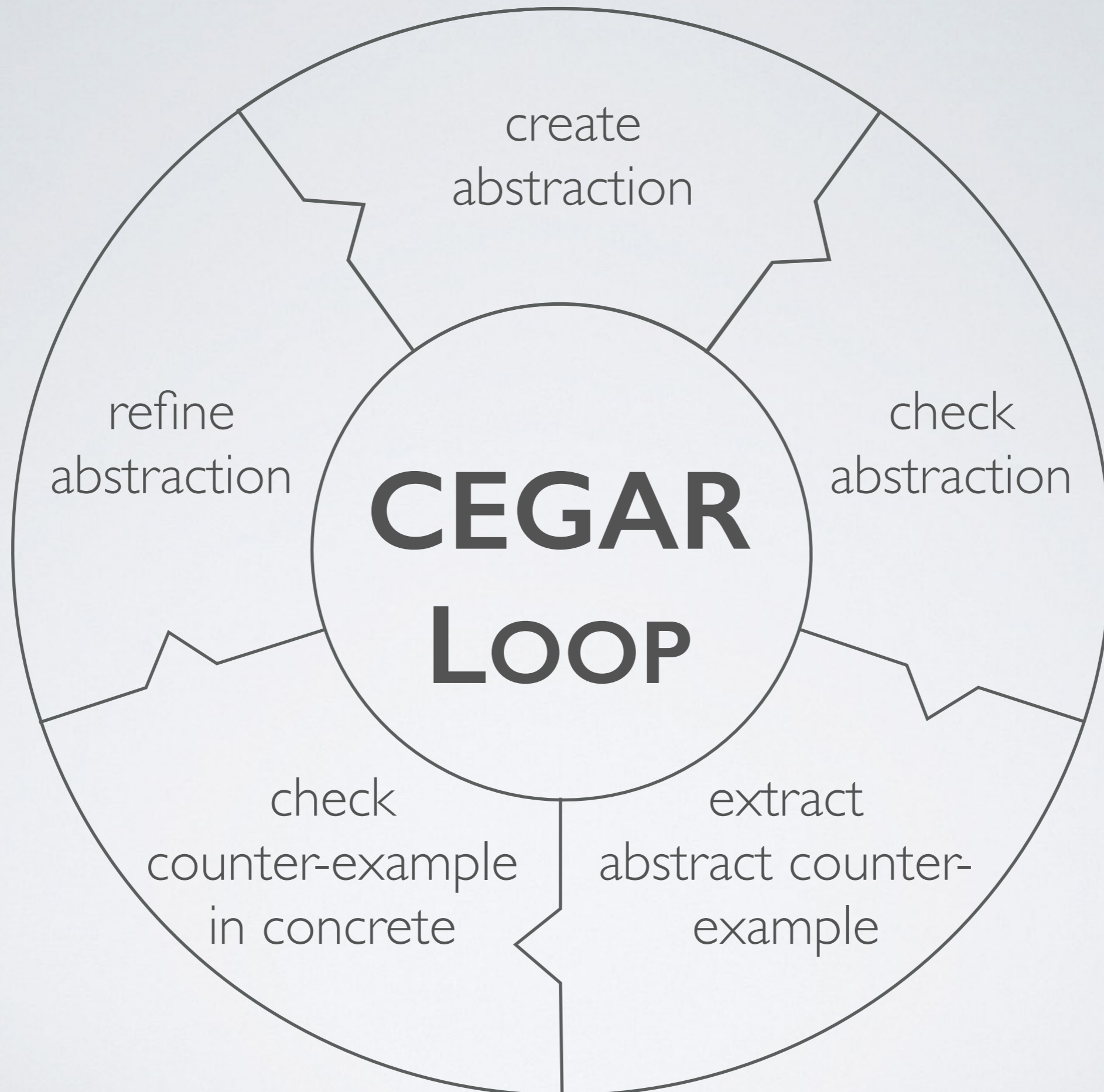
- ▶ state space exploration
 - ▶ control locations, variable values, ...
 - ▶ is there a bad state?
- ▶ multiple challenges

CHALLENGES

- ▶ unbounded recursion
- ▶ infinite data types
- ▶ unbounded heap
- ▶ specification
- ▶ ...

CHALLENGES

- ▶ **unbounded recursion**
- ▶ **infinite data types**
- ▶ unbounded heap
- ▶ **specification \leadsto by assertions**
- ▶ ...



**CEGAR
LOOP**

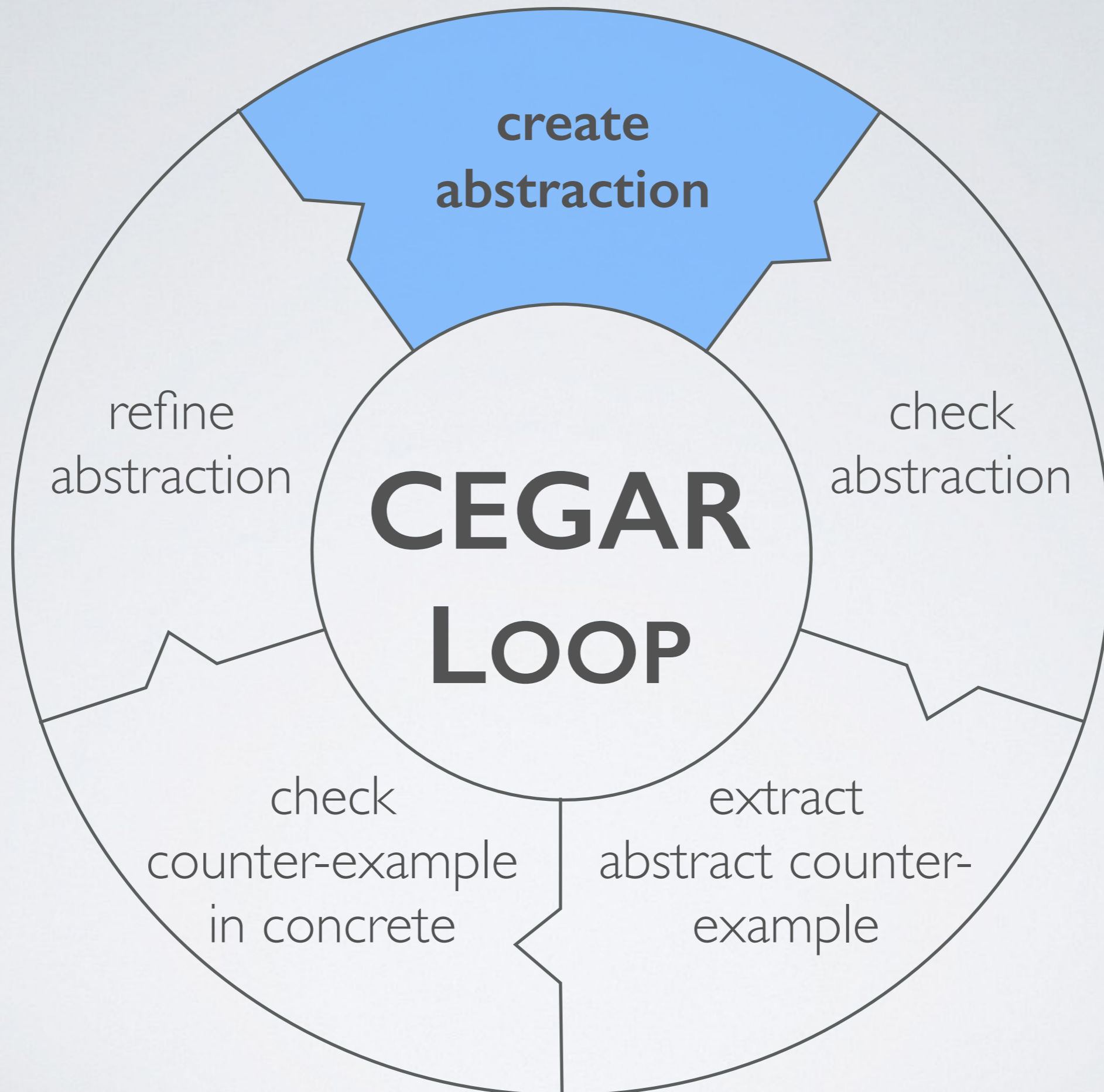
create
abstraction

check
abstraction

extract
abstract counter-
example

check
counter-example
in concrete

refine
abstraction



**create
abstraction**

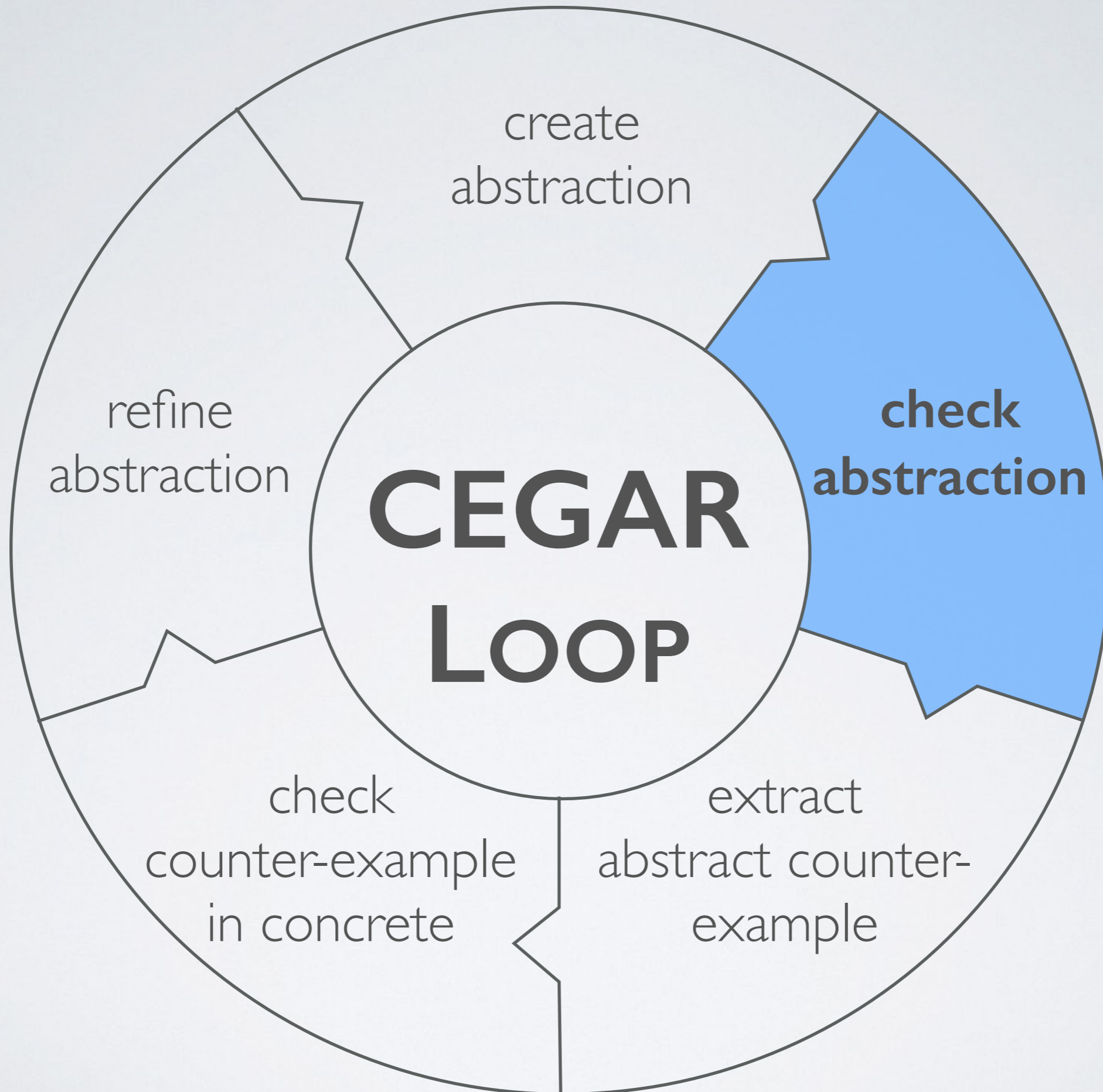
refine
abstraction

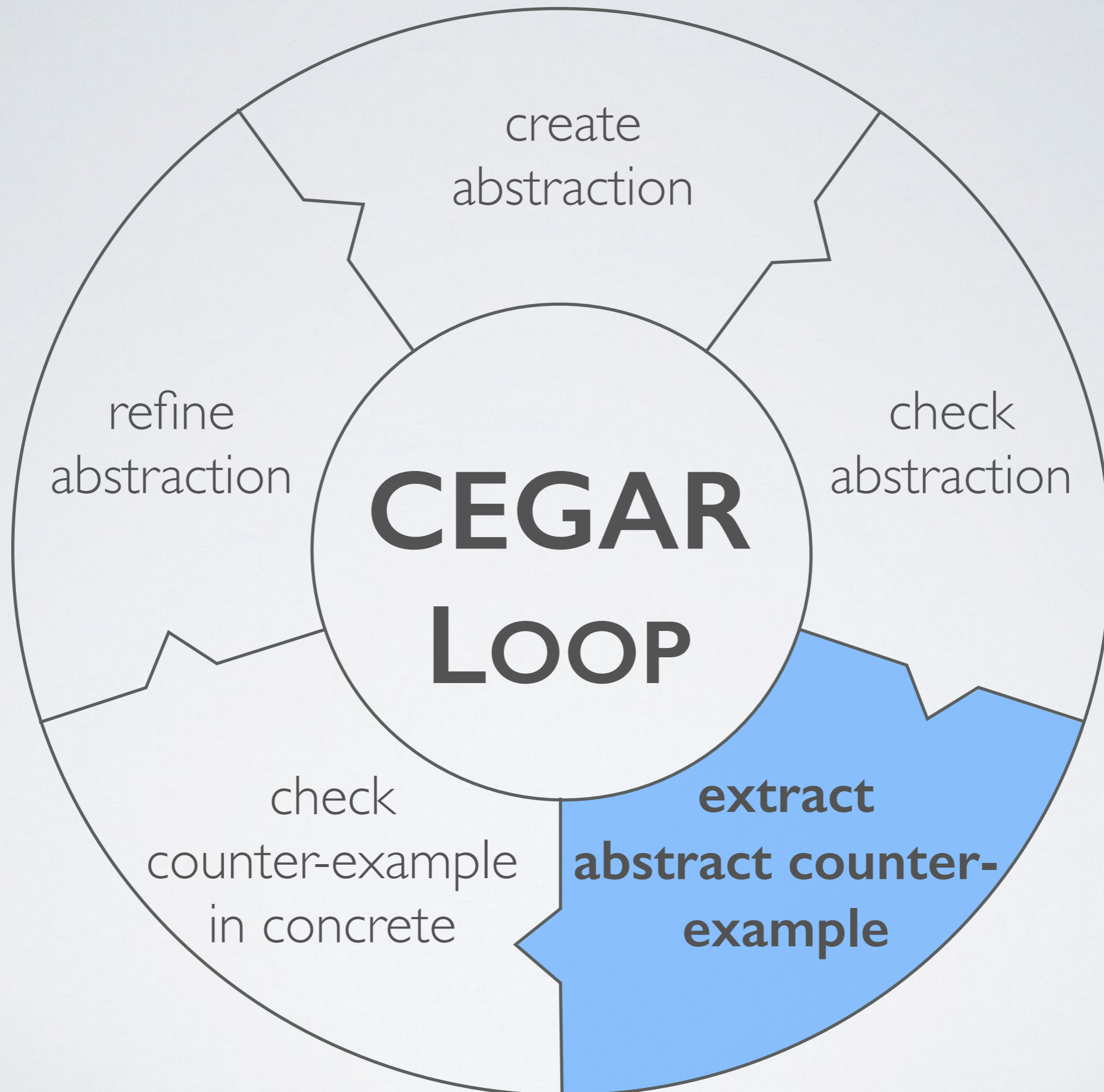
check
abstraction

**CEGAR
LOOP**

check
counter-example
in concrete

extract
abstract counter-
example





CEGAR LOOP

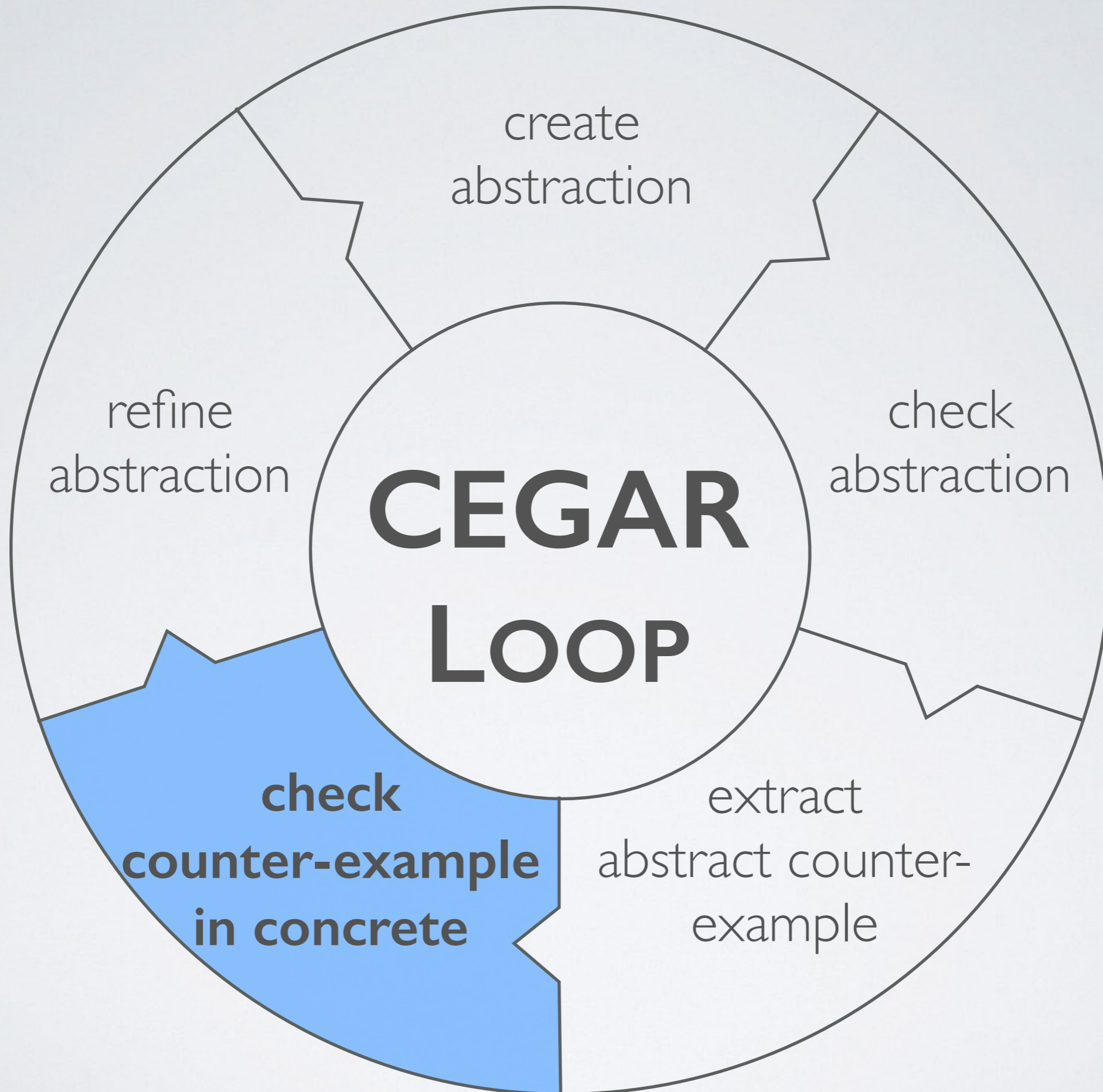
create
abstraction

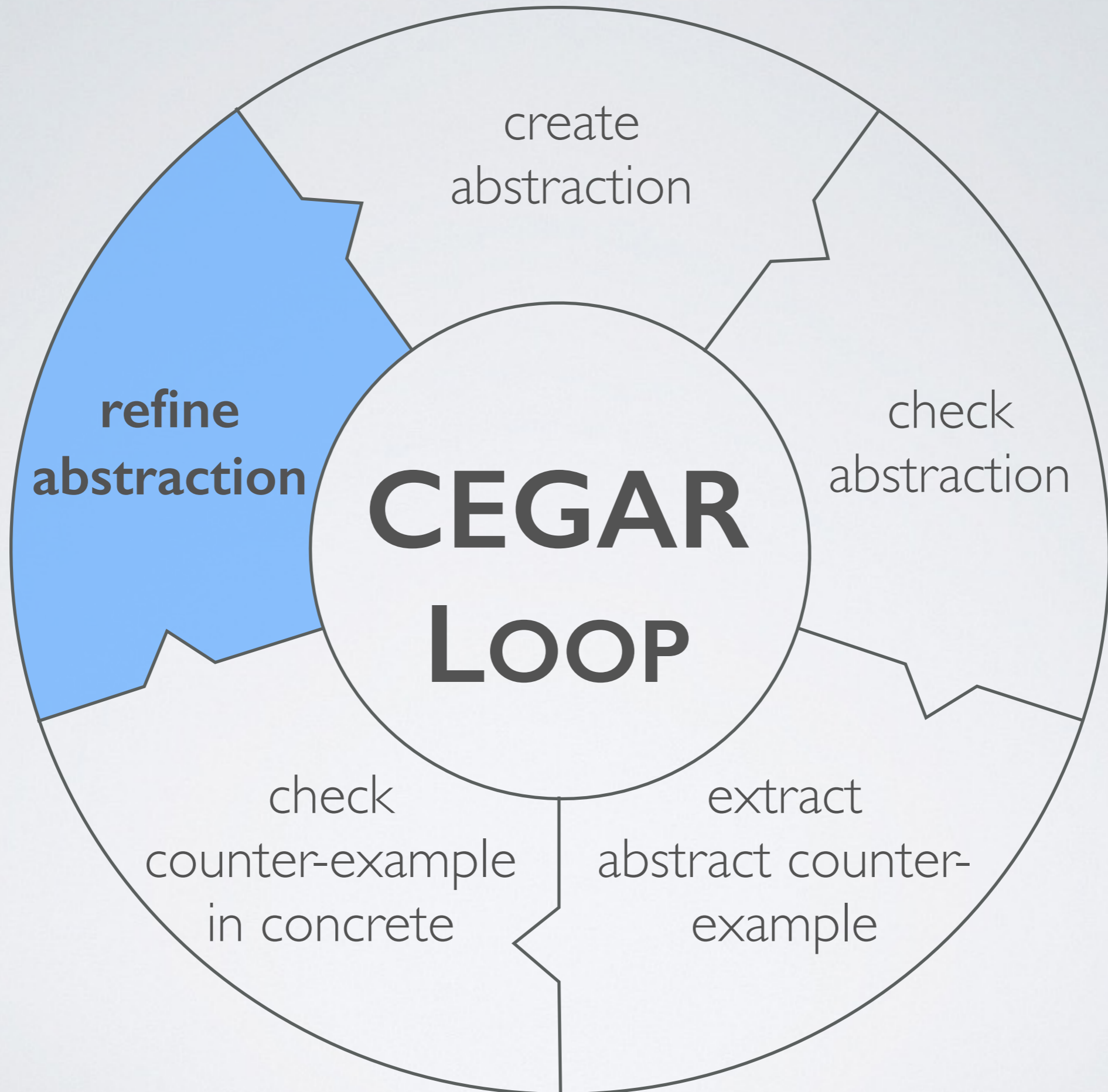
check
abstraction

**extract
abstract counter-
example**

check
counter-example
in concrete

refine
abstraction





PREDICATE ABSTRACTION

- ▶ aim: from infinite to finite
- ▶ don't track values
- ▶ track *useful* relations among values
- ▶ predicates evaluate to *true* or *false*



PREDICATE ABSTRACTION

```
int x, y;

void main() {
    // ...
    x = x - 1;
    if (x <= y)
        swap();
    assert(x >= y);
}

void swap() { ... }
```

```
bool p1; // x <= y

void main() {
    // ...
    p1 = p1 ? p1 : *;
    if (p1)
        swap();
    assert(!p1);
}

void swap() { ... }
```



PREDICATE ABSTRACTION

```
int x, y;
```

```
void main() {  
    // ...  
    x = x - 1;  
    if (x <= y)  
        swap();  
    assert(x >= y);  
}
```

```
void swap() { ... }
```

```
bool p1; // x <= y
```

```
void main() {  
    // ...  
    p1 = p1 ? p1 : *;  
    if (p1)  
        swap();  
    assert(!p1);  
}
```

```
void swap() { ... }
```



PREDICATE ABSTRACTION

```
int x, y;

void main() {
    // ...
    x = x - 1;
    if (x <= y)
        swap();
    assert(x >= y);
}

void swap() { ... }
```

```
bool p1; // x <= y

void main() {
    // ...
    p1 = p1 ? p1 : *;
    if (p1)
        swap();
    assert(!p1);
}

void swap() { ... }
```



PREDICATE ABSTRACTION

```
int x, y;

void main() {
    // ...
    x = x - 1;
    if (x <= y)
        swap();
    assert(x >= y);
}

void swap() { ... }
```

```
bool p1; // x <= y

void main() {
    // ...
    p1 = p1 ? p1 : *;
    if (p1)
        swap();
    assert(!p1);
}

void swap() { ... }
```



PREDICATE ABSTRACTION

```
int x, y;

void main() {
    // ...
    x = x - 1;
    if (x <= y)
        swap();
    assert(x >= y);
}

void swap() { ... }
```

```
bool p1; // x <= y

void main() {
    // ...
    p1 = p1 ? p1 : *;
    if (p1)
        swap();
    assert(!p1);
}

void swap() { ... }
```



CHECK FOR CORRECTNESS

- ▶ reduce to reachability check
 - ▶ translate to control flow graph
 - ▶ bad state reachable?
- ▶ procedure summaries (skipped)



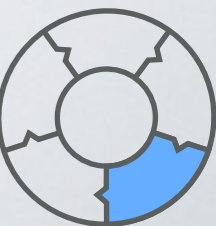
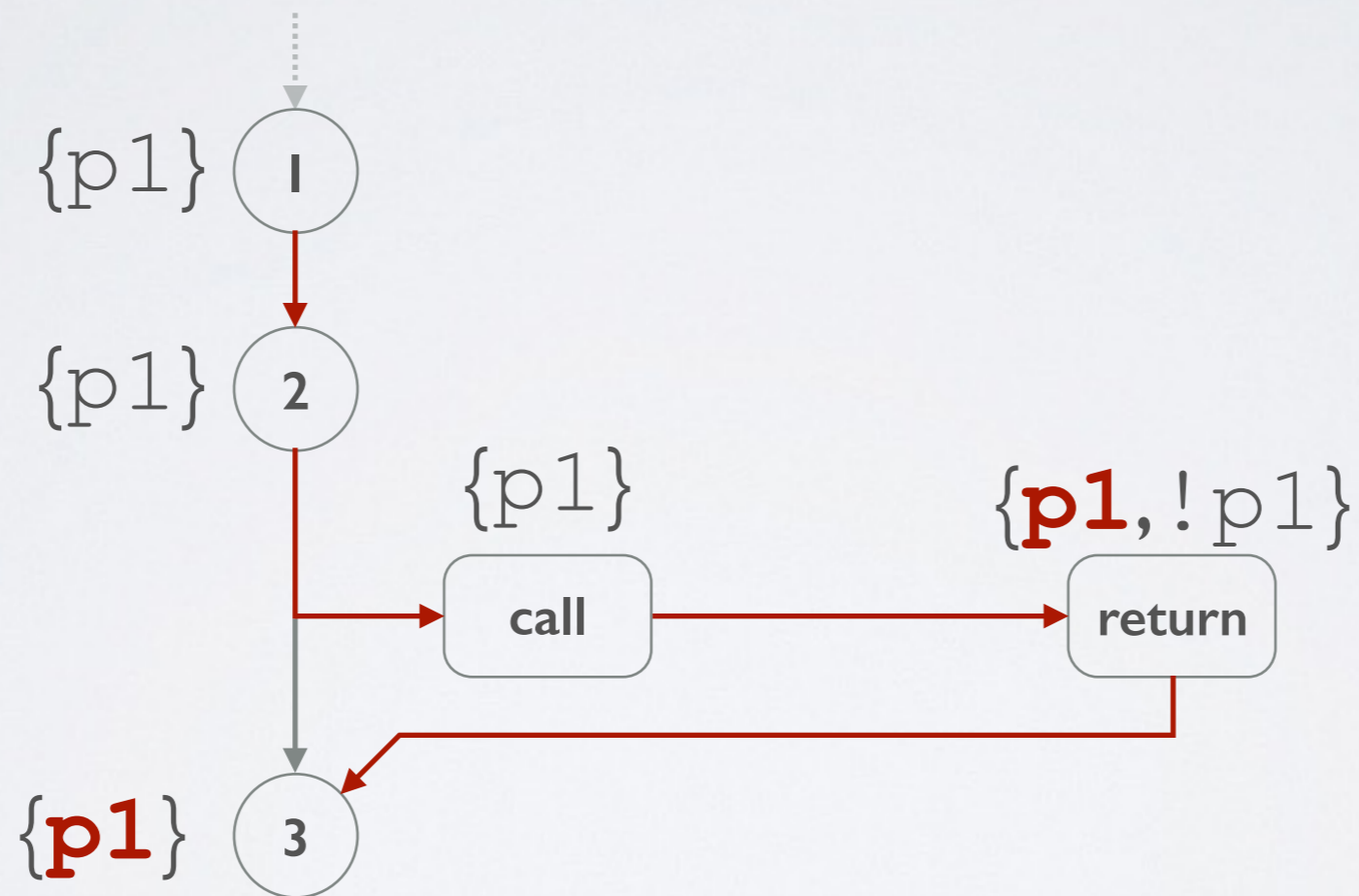
EXAMPLE

```
void main() {  
    // ...  
    1 p1 = p1 ? p1 : *;  
    2 if (p1)  
        call swap();  
        return  
    3 assert(!p1);  
}  
void swap() { ... }
```

```
graph TD; Start(( )) -.-> Node1((1)); Node1 --> Node2((2)); Node2 --> Node3((3)); Node2 --> Call[call swap()]; Call -- return --> Node3;
```



EXTRACT COUNTER-EXAMPLE



CHECK FEASIBILITY

- ▶ counter-example trace possible?
 - ▶ judge in original program
- ▶ weakest preconditions
 - ▶ $\{true\}$ trace $\{false\}$ valid Hoare triple?



EXAMPLE

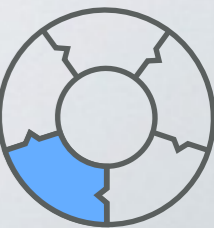
```
x = x - 1;
```

```
if (x <= y)
```

```
    swap ();
```

fails in
counter-
example

```
    assert (x >= y) ;
```



EXAMPLE

```
x = x - 1;  
if (x <= y)  
    // x > y  
    swap ();  
  
    // x < y  
    assert (x >= y) ;
```

fails in
counter-
example



EXAMPLE

```
x = x - 1;  
if (x <= y)  
    // x > y  
    swap();  
  
// x < y  
assert(x >= y);
```

fails in
counter-
example



REFINE ABSTRACTION

- ▶ abstraction too imprecise
- ▶ need new/better predicates
- ▶ remove spurious counter-example
- ▶ Craig interpolation



THERE'S A PROTOTYPE

- ▶ ~5500 line C++ code
 - ▶ CUDD BDD library
 - ▶ Z3 SMT solver
- ▶ >90% time spend on generating abstractions

— FIN —

BACKUP SLIDES

FULL WP-EXAMPLE

```
{true}
```

```
x = x - 1;
```

```
{x <= y ∨ x > y}
```

```
assume (x <= y)
```

```
{x <= y}
```

```
swap();
```

```
{false ∨ x >= y}
```

```
assume (x < y);
```

```
{false}
```

```
assert (false);
```

```
{false}
```



PROCEDURE SUMMARIES

- ▶ sub-analysis for function calls
- ▶ extend CFG with summary edges
 - ▶ impact of function to global variables
 - ▶ on demand
- ▶ termination check (!)



EXAMPLE

